## CLAIMS

 An encryption method, comprising the steps of: dividing a plaintext to be encrypted thereby to obtain a plaintext vector;

applying a predetermined transformation on the plaintext vector thereby to generate a transformation vector; and

generating a ciphertext by a product-sum operation between the components of a public key vector and the components of the plaintext vector and the transformation vector.

- 2. The encryption method of Claim 1, wherein the product sum operation with the components of the public key vector is performed using alternately a component of the plaintext vector and a component of the transformation vector.
- The encryption method of Claim 1, wherein the public key vector is obtained by a modulo transformation of a base-product vector.
- 4. The encryption method of Claim 1, wherein: the components of the plaintext vector and the transformation vector are expressed by  $(m_1, m_2, ..., m_K)$ ; the components of the public key vector are obtained by a modulo transformation of the components  $B_i$  of a base-product vector  $(B_1, B_2, ..., B_K)$  (where  $B_i = v_i$   $b_1$   $b_2$  ...  $b_i$ , with random numbers  $v_i$  and bases  $b_i$   $(1 \le i \le K)$ ); and as the bases  $b_i$  a normal base satisfying  $b_i$   $b_i$  is used when the  $m_{i+1}$  is a component of the plaintext vector while a reduced base satisfying  $b_i$   $b_i$   $b_i$  is used when the  $b_i$  is a

component of the transformation vector.

5. An encryption method, comprising the step of generating a product sum type ciphertext using a first vector depending on a plaintext and a second vector having components obtained by a modulo transformation of base products; wherein

the first vector is composed of a plaintext vector obtained by dividing a plaintext to be encrypted; and a transformation vector obtained by a transformation of the plaintext vector using a predetermined function; and wherein the base product is obtained by both normal bases satisfying  $b_i > m_{i\cdot 1}$  ( $b_i$  is a base in the base product,  $m_{i\cdot 1}$  is a component of the first vector, i is an element of a subset S of a universal set  $U = \{2,3,...,K\}$ , and K is the number of components of the first and second vector) and reduced bases satisfying  $b_i \leq m_{j\cdot 1}$  ( $b_i$  is a base in the base product,  $m_{j\cdot 1}$  is a component of the first vector, and j is an element of a complementary set of the subset S).

- 6. A decryption method for decrypting a ciphertext generated by the encryption method of Claim 1, wherein the transformation vector is decrypted depending on decrypted components of the plaintext vector.
- 7. A decryption method for decrypting a ciphertext generated by the encryption method of Claim 2, wherein the transformation vector is decrypted depending on decrypted components of the plaintext vector.
  - 8. A decryption method for decrypting a ciphertext generated

by the encryption method of Claim 3, wherein the transformation vector is decrypted depending on decrypted components of the plaintext vector.

- 9. A decryption method for decrypting a ciphertext generated by the encryption method of Claim 4, wherein the transformation vector is decrypted depending on decrypted components of the plaintext vector.
- 10. A decryption method for decrypting a ciphertext generated by the encryption method of Claim 4, wherein a reduced-base part is decrypted depending on a decrypted normal-base part.
- 11. A decryption method for decrypting a ciphertext generated by the encryption method of Claim 5, wherein a reduced base part is decrypted depending on a decrypted normal base part.
- 12. A cryptographic communication system for communicating information by a ciphertext between entities, comprising:
- an encryptor for generating a ciphertext from a plaintext in accordance with the encryption method of Claim 1;
- a communication channel for transmitting the generated ciphertext from one entity to another entity; and
- a decryptor for decrypting the transmitted ciphertext into a  $\mbox{plaintext}.$ 
  - 13. A cryptographic communication system for

communicating information by a ciphertext between entities, comprising:

an encryptor for generating a ciphertext from a plaintext in accordance with the encryption method of Claim 2;

a communication channel for transmitting the generated ciphertext from one entity to another entity; and

a decryptor for decrypting the transmitted ciphertext into a plaintext.

14. A cryptographic communication system for communicating information by a ciphertext between entities, comprising:

an encryptor for generating a ciphertext from a plaintext in accordance with the encryption method of Claim 3;

a communication channel for transmitting the generated ciphertext from one entity to another entity; and

a decryptor for decrypting the transmitted ciphertext into a plaintext.

15. A cryptographic communication system for communicating information by a ciphertext between entities, comprising:

an encryptor for generating a ciphertext from a plaintext in accordance with the encryption method of Claim 4;

a communication channel for transmitting the generated ciphertext from one entity to another entity; and

a decryptor for decrypting the transmitted ciphertext into a

plaintext.

16. A cryptographic communication system for communicating information by a ciphertext between entities, comprising:

an encryptor for generating a ciphertext from a plaintext in accordance with the encryption method of Claim 5;

a communication channel for transmitting the generated ciphertext from one entity to another entity; and

a decryptor for decrypting the transmitted ciphertext into a plaintext.

- 17. An encryption device for generating a product sum type ciphertext from a plaintext, comprising a controller capable of performing the operations of:
- (i) dividing a plaintext to be encrypted thereby to obtain a plaintext vector;
- $\mbox{(ii) applying a predetermined transformation on the} \\$  plaintext vector thereby to generate a transformation vector; and
- (iii) generating a ciphertext by a product sum operation between the components of a public key vector and the components of the plaintext vector and the transformation vector.
- 18. A computer memory product having computer readable program code means for causing a computer to generate a product-sum type ciphertext from a plaintext, said computer readable program code means comprising:

program code means for causing the computer to divide a

plaintext to be encrypted thereby to obtain a plaintext vector;

program code means for causing the computer to apply a predetermined transformation on the plaintext vector thereby to generate a transformation vector; and

program code means for causing the computer to generate a ciphertext by a product sum operation between the components of a public key vector and the components of the plaintext vector and the transformation vector.

19. A computer data signal embodied in a carrier wave for transmitting a program, the program being configured to cause a computer to generate a product sum type ciphertext from a plaintext, comprising:

a code segment for causing the computer to divide a plaintext to be encrypted thereby to obtain a plaintext vector;

a code segment for causing the computer to apply a predetermined transformation on the plaintext vector thereby to generate a transformation vector; and

a code segment for causing the computer to generate a ciphertext by a product sum operation between the components of a public key vector and the components of the plaintext vector and the transformation vector.